On Solvability of Sylvester Equation via Coupled Fixed Point

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In this paper, we will study existence and uniqueness of solution to Sylvester equation

$$AX - XB = C$$

where C is hermetian positive definite matrix and A, B an arbitrary matrices, by using coupled fixed point technique.

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