

## Multiplicity of Periodic Solutions for $2n^{\text{th}}$ -order $p$ -Laplacian Differential Equations

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**2010 MSC:** 34B15

This is a joint work with Dr. L. Saavedra. We study the existence and multiplicity of weak and classic solutions for a  $2n^{\text{th}}$ -order differential equation involving the  $p$ -Laplacian

$$(1) \quad \left( \varphi_p \left( u^{(n)}(t) \right) \right)^{(n)} + \sum_{i=1}^{n-1} (-1)^i a_i \left( \varphi_p \left( u^{(n-i)}(t) \right) \right)^{(n-i)} \\ + (-1)^n (f(t, u(t)) - h(t, u(t))) = 0, \quad t \in [0, T]$$

coupled with the periodic boundary conditions

$$(2) \quad u(T) - u(0) = \dots = u^{(2n-1)}(T) - u^{(2n-1)}(0) = 0,$$

where  $T \geq 0$  and  $a_i \geq 0$  for  $i = 1, \dots, n-1$ . The results are proved by using the minimization argument and an extended Clark's theorem. The second-order equations are considered in [1]. The results are published in [2].

## References

- [1] P. Drábek, M. Langerová, S. Tersian, Existence and multiplicity of periodic solutions to one-dimensional  $p$ -Laplacian, *Electronic Journal of Qualitative Theory of Differential Equations*, 30 (2016) 1–9.
- [2] L. Saavedra, S. Tersian, Existence of solutions for 2nd-order nonlinear  $p$ -Laplacian differential equations *Nonlinear Analysis: Real World Applications*, 34 (2017) 507–519.